

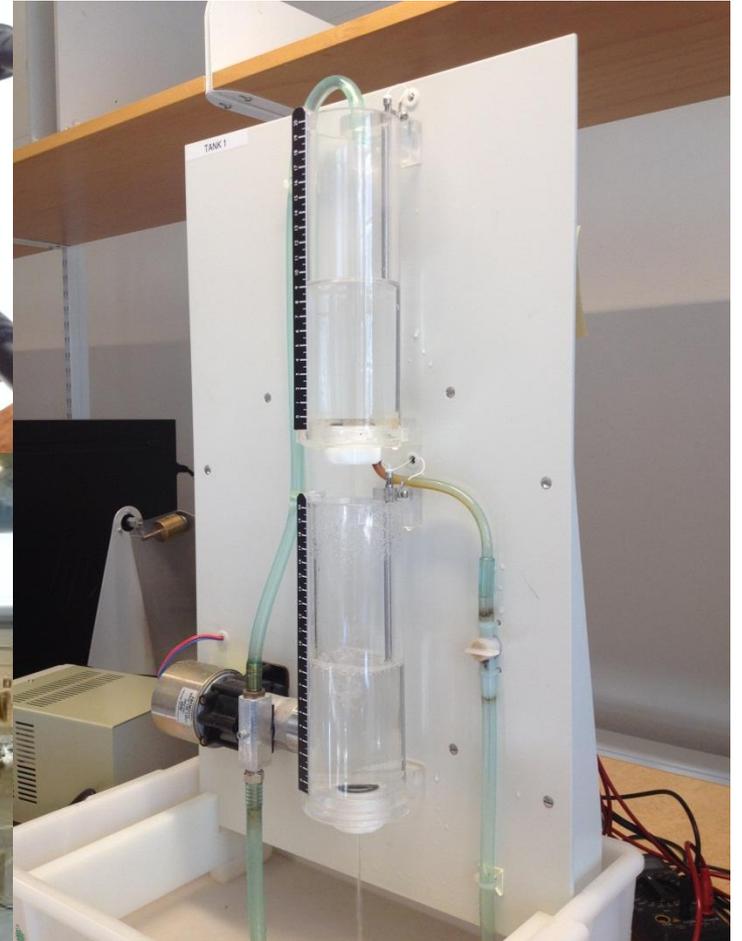
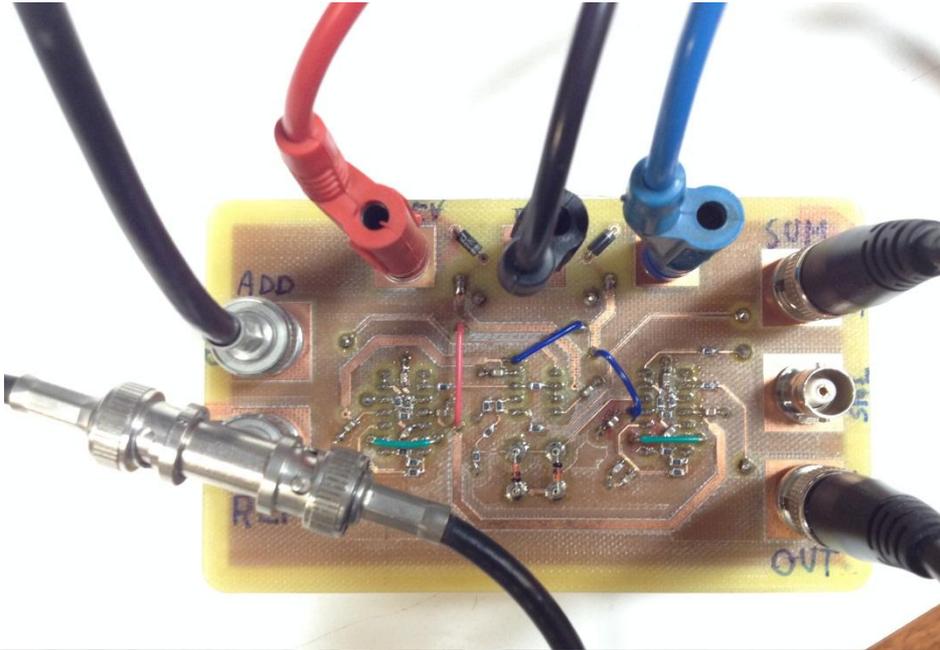
# Challenging Ourselves: Three Benchmarks for Nonlinear System Identification

Maarten Schoukens (VUB)  
Jean-Philippe Noël (ULg)



Vrije  
Universiteit  
Brussel





# Benchmark on nonlinear system identification

Raise interest in selected challenges

Compare methods

Interaction between identification communities

Mechanical

Systems & Control

Machine Learning



Benchmark Workshop, Spring 2016

# Outline

## Benchmarks

What? Why? How?

Challenges in nonlinear sys. id.

Three benchmarks

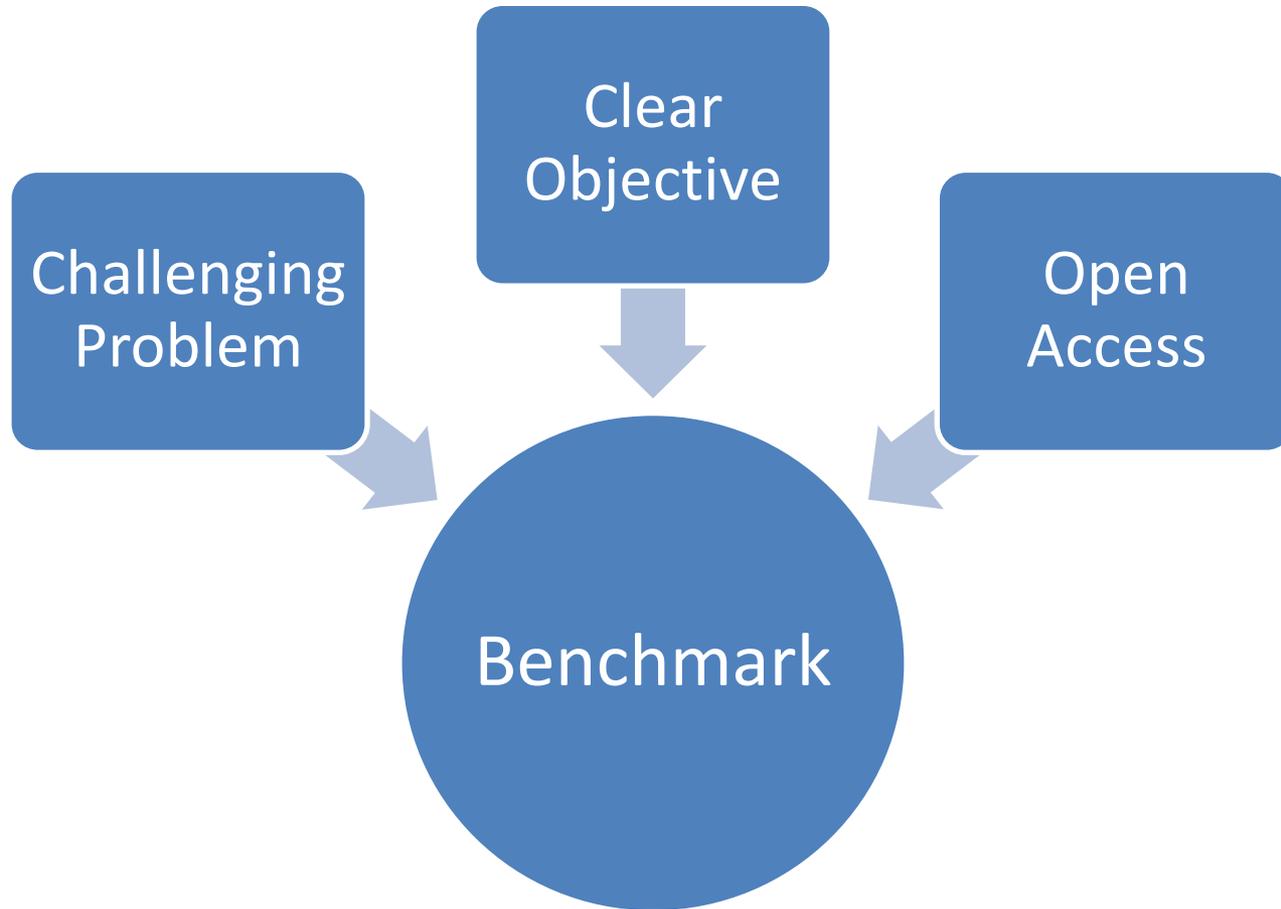
Bouc-Wen

Wiener-Hammerstein

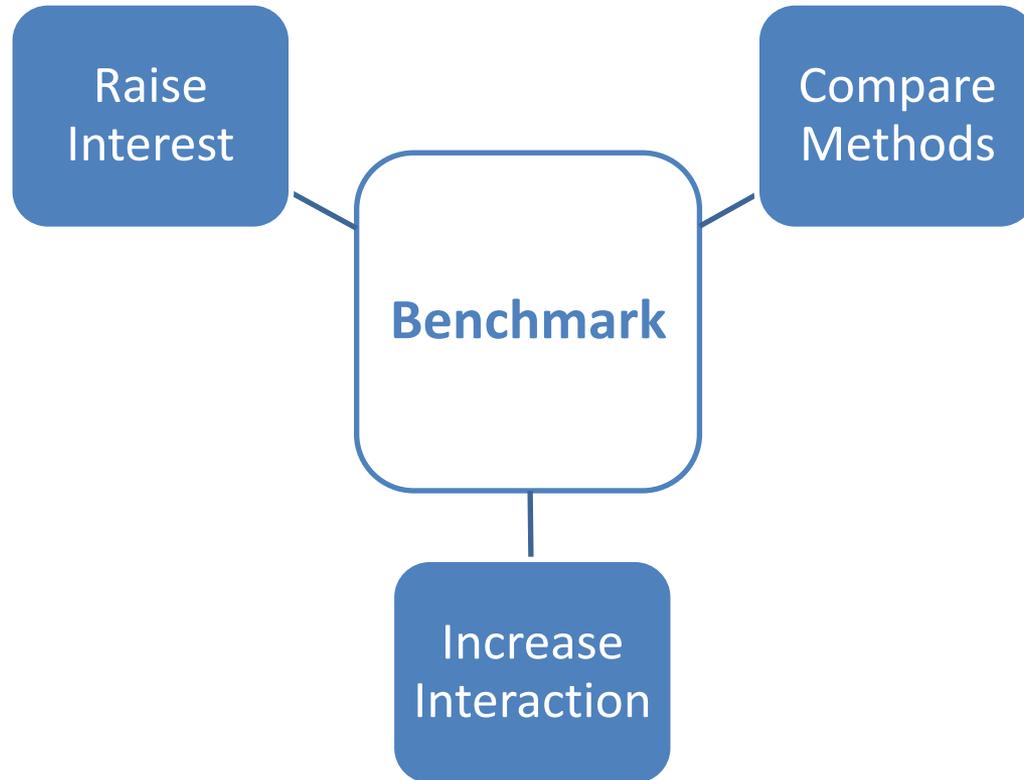
Cascaded Tanks

Benchmark meeting: practicalities

# Benchmarks: What?



# Benchmarks: Why?



# Benchmarks: How?

System

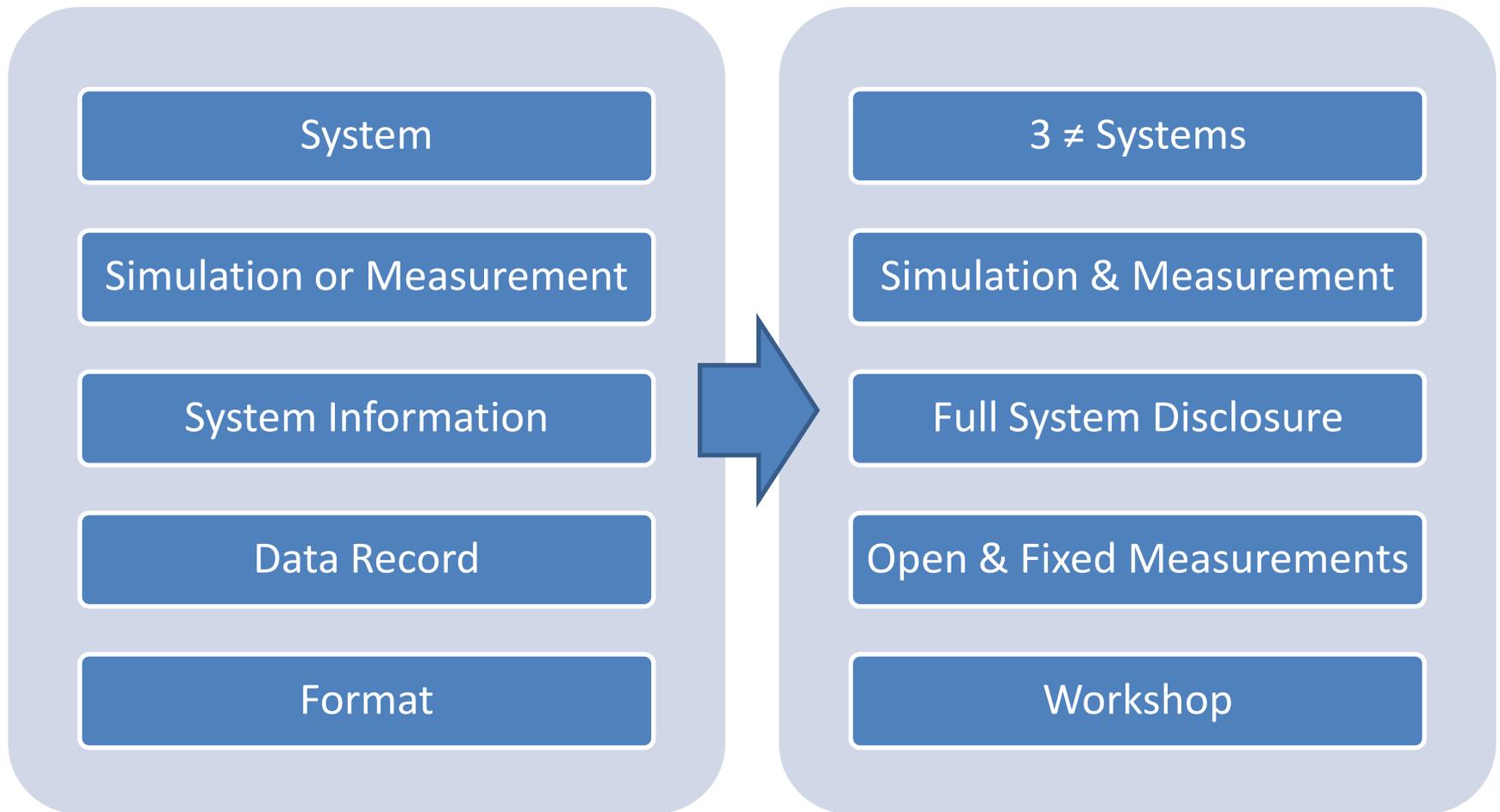
Simulation or Measurement

System Information

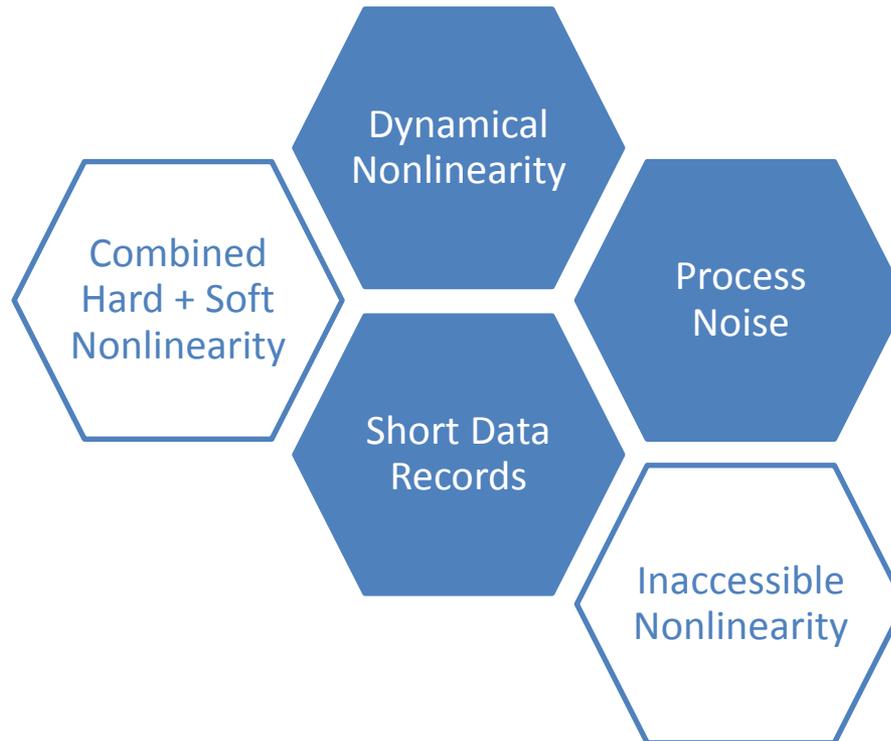
Data Record

Format

# Benchmarks: How?



# Nonlinear Sys Id: Challenges



# Three Benchmarks

Bouc-Wen

- Hysteresis

Wiener-  
Hammerstein

- Process Noise

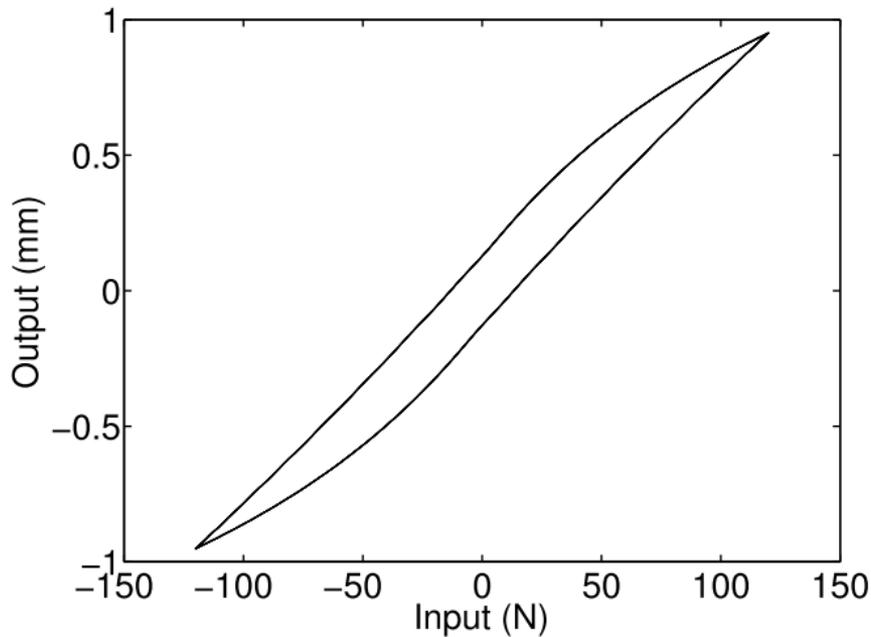
Cascaded  
Tanks

- Short Data Record

# Bouc-Wen Hysteretic System



# Bouc-Wen Hysteretic System



Nonlinear differential equations:

$$m_L \ddot{y}(t) + r(y, \dot{y}) + z(y, \dot{y}) = u(t)$$

$$r(y, \dot{y}) = k_L y + c_L \dot{y}$$

$$\dot{z}(y, \dot{y}) = \alpha \dot{y} - \beta (\gamma |\dot{y}| z + \delta \dot{y} |z|)$$



Nonlinearity with memory

# Bouc-Wen Hysteretic System

What do we provide?

Matlab simulation package

Signal design by participants

As much data as you want

Available on benchmark website

Noiseless validation

# Bouc-Wen Hysteretic System

## Challenges:

Nonlinearity with memory

Nonlinearity governed by internal variable

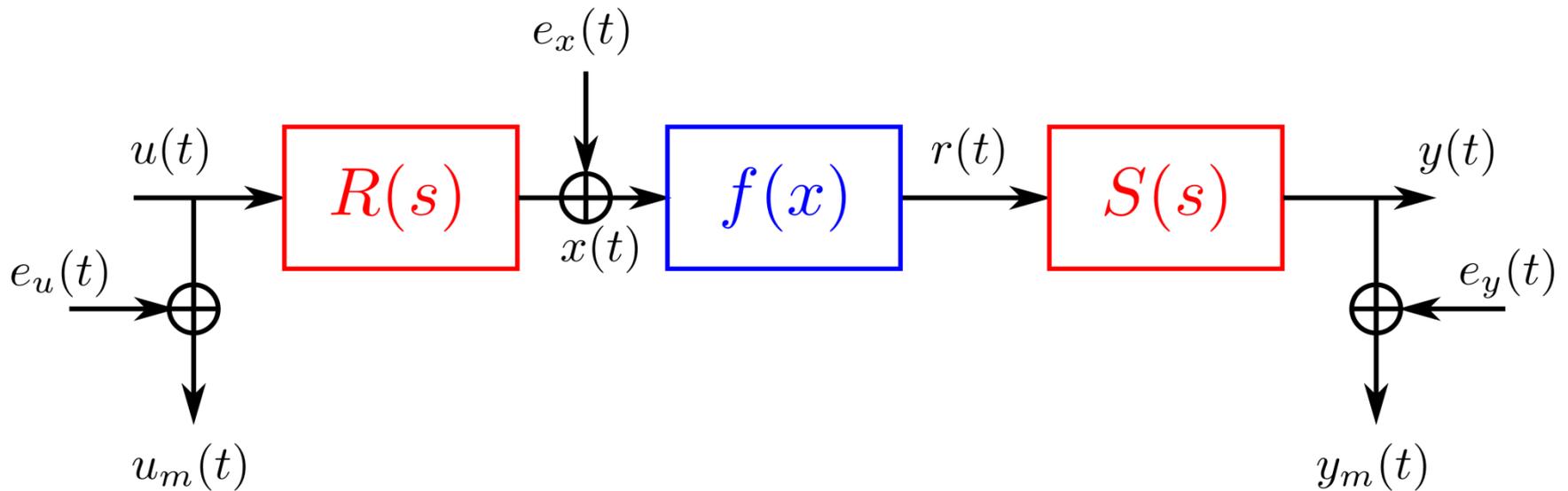
Nonlinearity is not differentiable

$$m_L \ddot{y}(t) + r(y, \dot{y}) + z(y, \dot{y}) = u(t)$$

$$r(y, \dot{y}) = k_L y + c_L \dot{y}$$

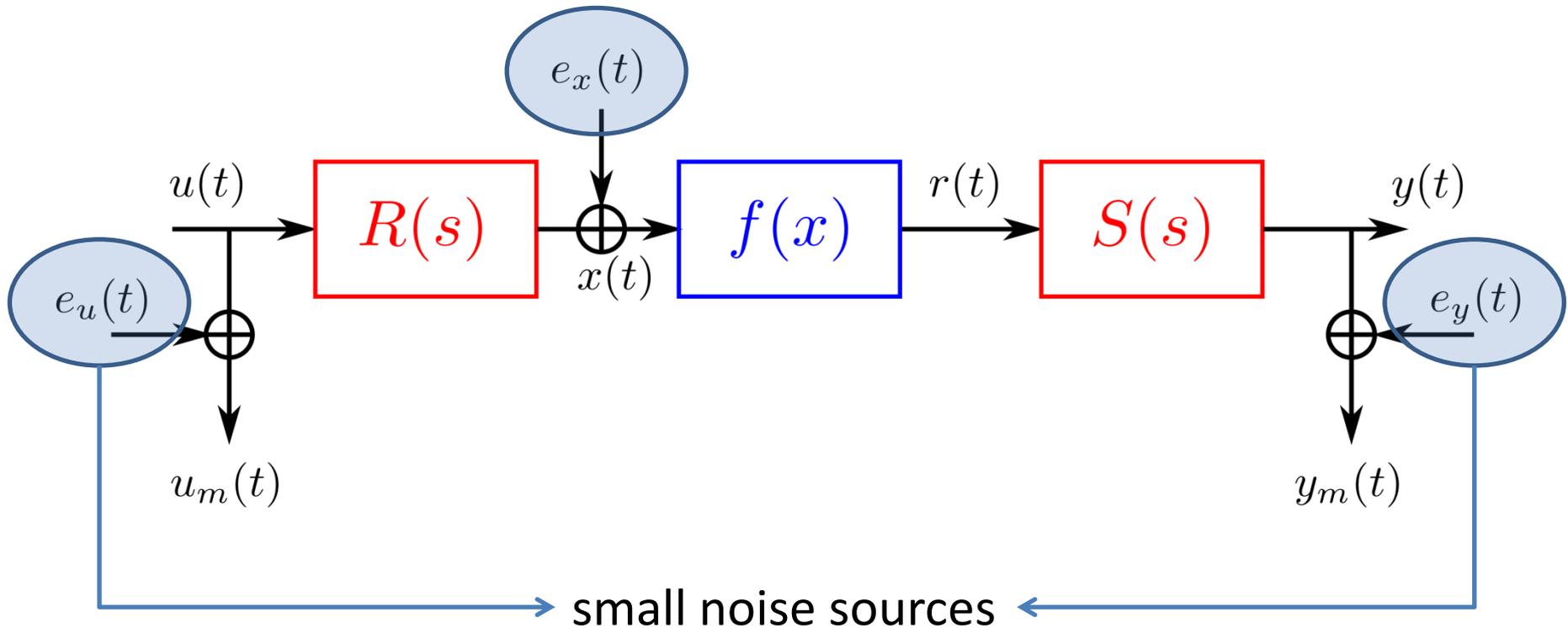
$$\dot{z}(y, \dot{y}) = \alpha \dot{y} - \beta(\gamma |\dot{y}| z + \delta \dot{y} |z|)$$

# Wiener-Hammerstein + Process Noise

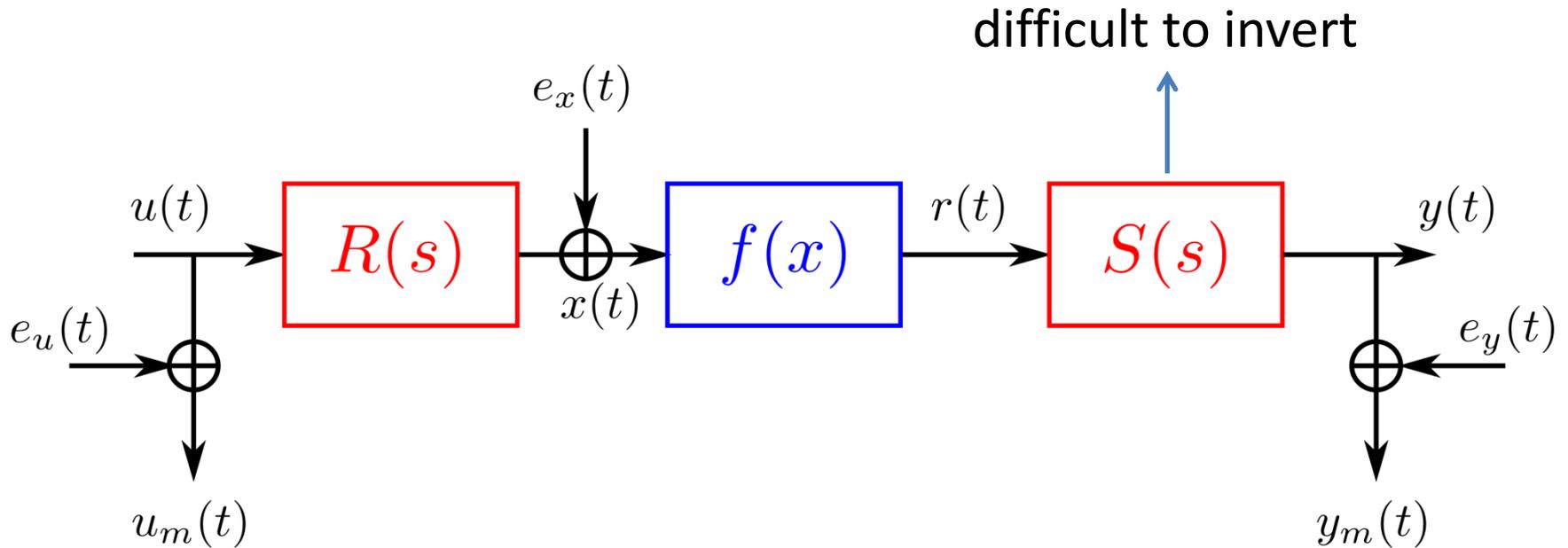


# Wiener-Hammerstein + Process Noise

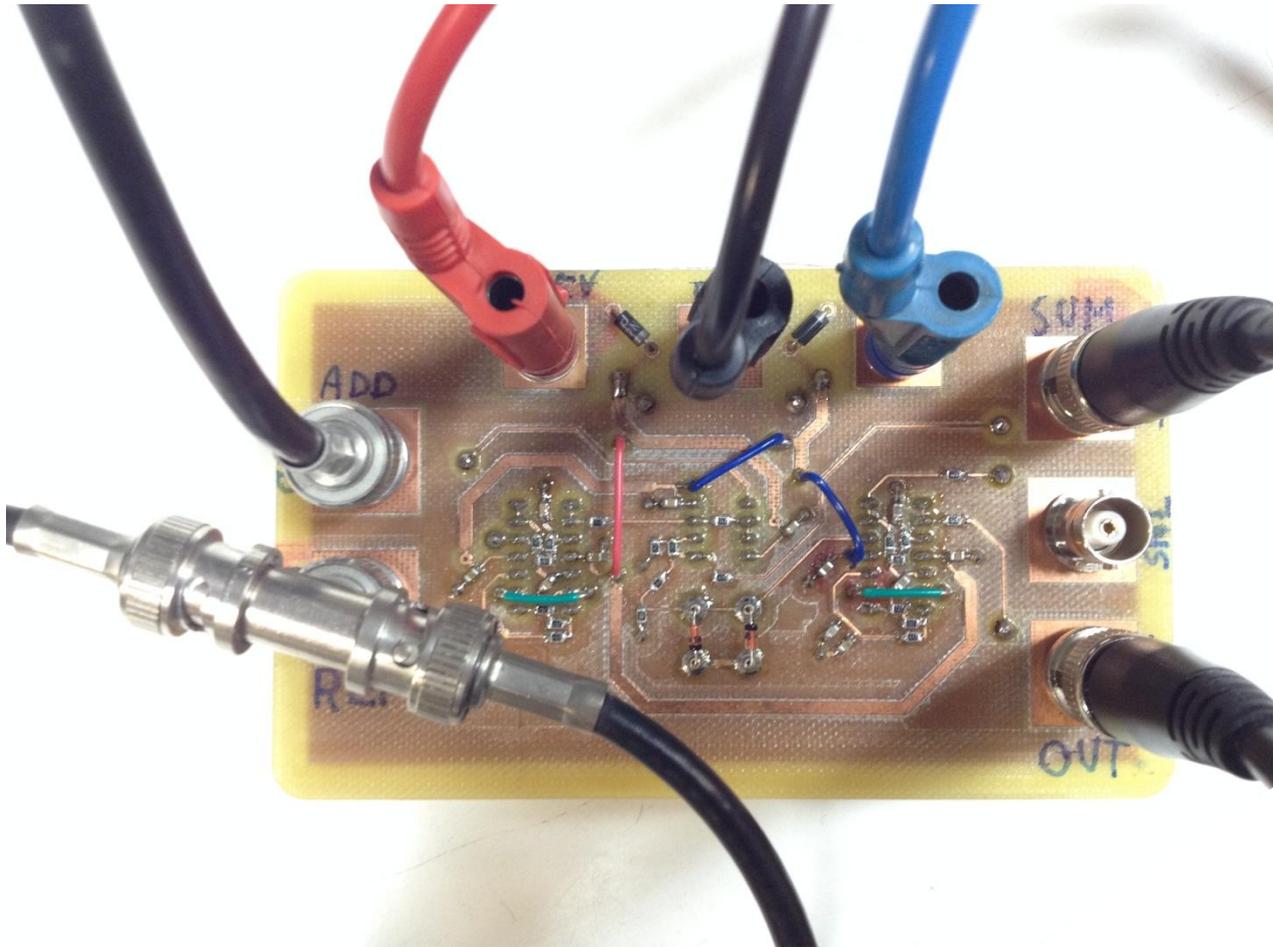
dominant noise source



# Wiener-Hammerstein + Process Noise



# Wiener-Hammerstein + Process Noise



# Wiener-Hammerstein + Process Noise

Open measurement campaigns:

Setup @ VUB, Brussels

Signal design by participants

Measurements performed by me

As much data as you want\*

All data available to all participants

Noiseless validation

\* Terms and conditions may apply ;)

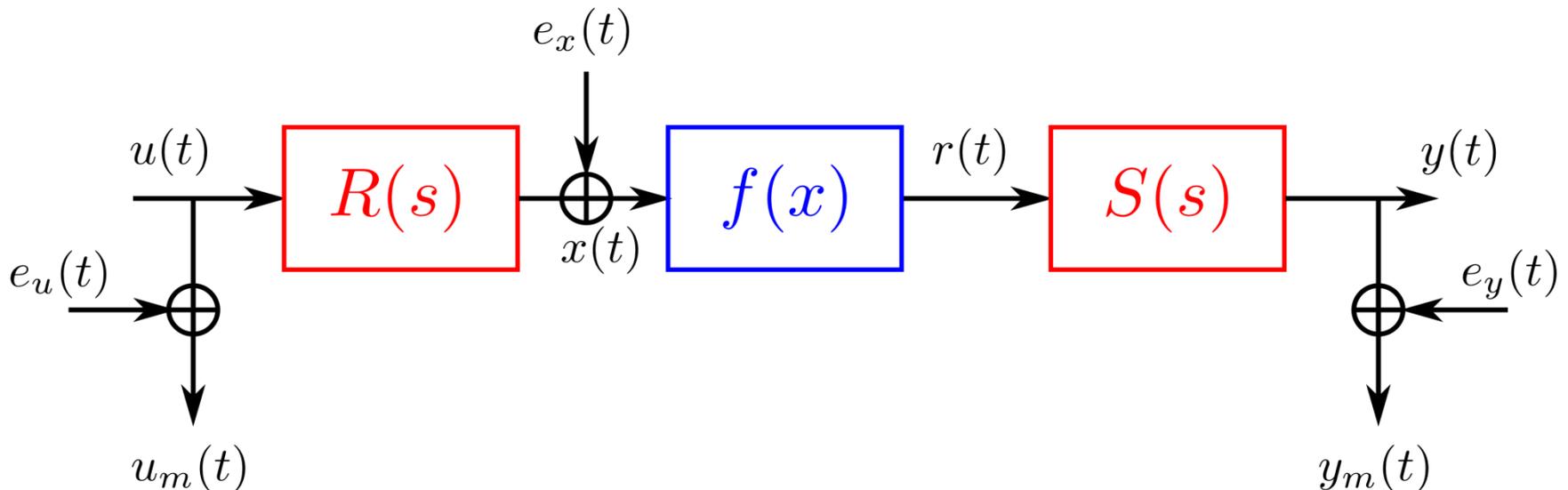
# Wiener-Hammerstein + Process Noise

## Challenges:

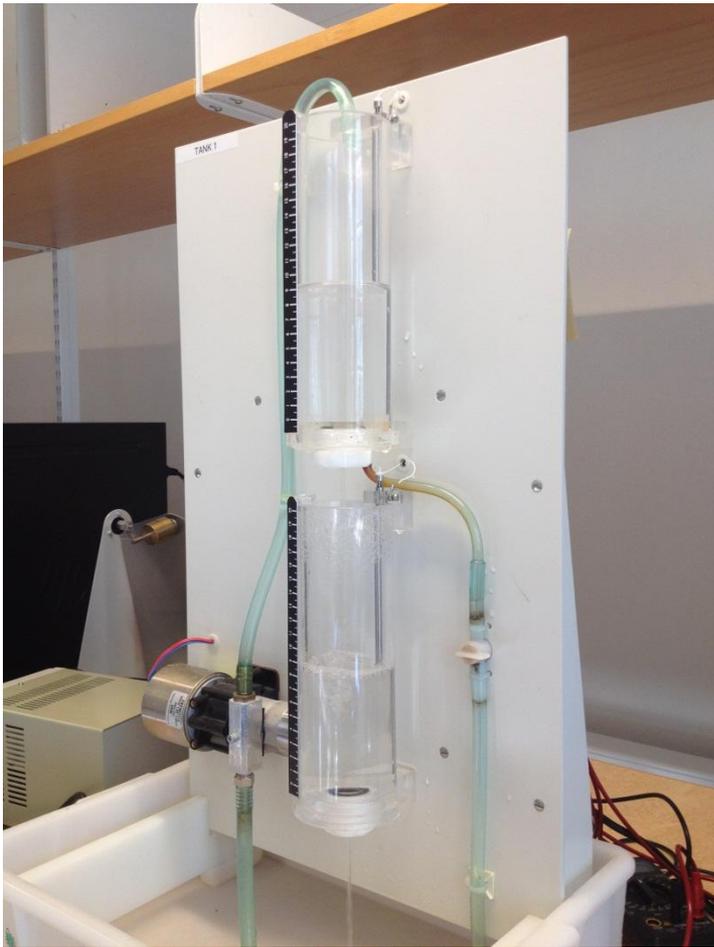
Process noise in nonlinear system

Nonlinearity not accessible from measurements

Output dynamics are difficult to invert



# Cascaded Tanks: Short Data Record



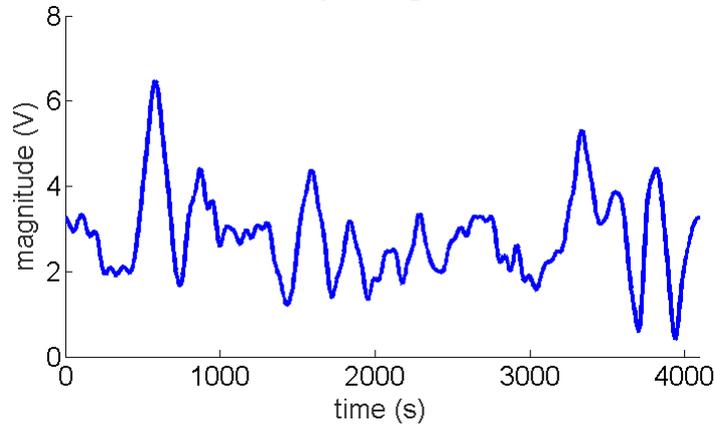
Nonlinear system dynamics:

$$\begin{aligned}\dot{x}_1(t) &= -k_1\sqrt{x_1(t)} + k_4u(t) + w_1(t), \\ \dot{x}_2(t) &= k_2\sqrt{x_1(t)} - k_3\sqrt{x_2(t)} + w_2(t), \\ y(t) &= x_2(t) + e(t),\end{aligned}$$

Overflow not included!

# Cascaded Tanks: Short Data Record

input signal



Fixed data records:

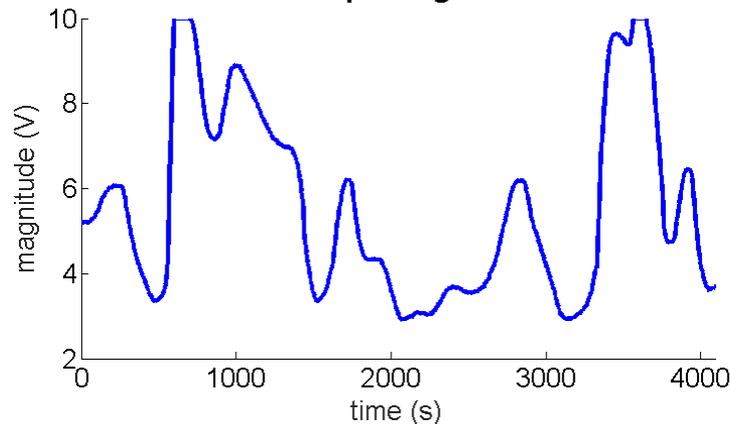
1024 points

60 frequencies excited

Unknown initial states

Small information content

output signal



# Cascaded Tanks: Short Data Record

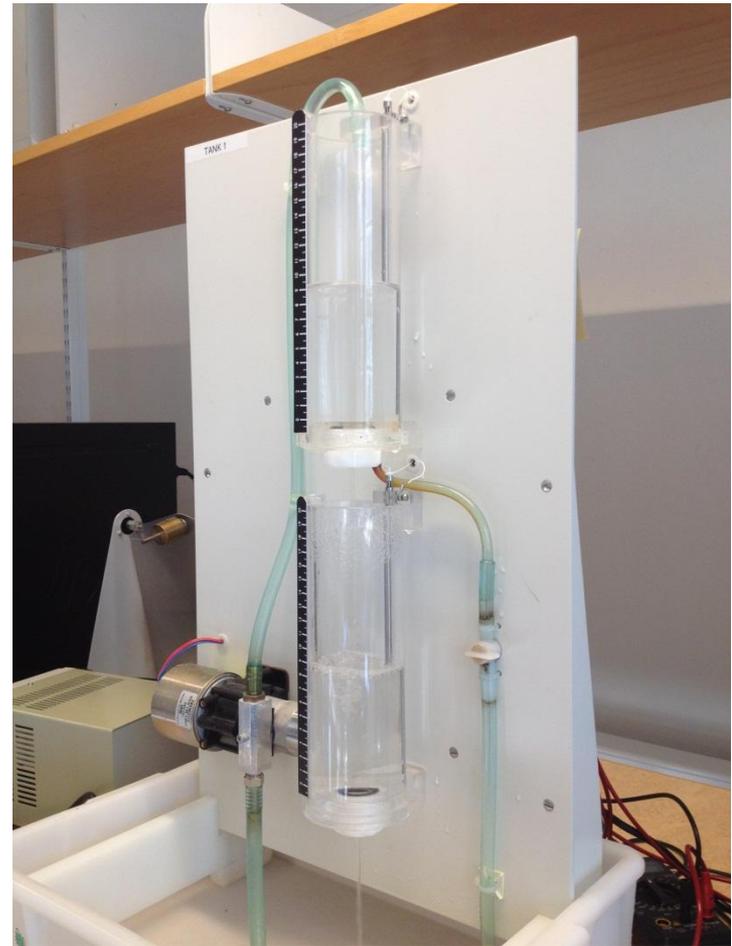
## Challenges:

Small information content

Combination of soft and hard nonlinearity

Overflow

Unknown initial states



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Benchmark Workshop, Spring 2016

# Benchmark: Practicalities

- When: 25/04/2016 – 27/04/2016
- Where: Brussels, Belgium
- Who: Mechanical, Systems & Control and  
Machine Learning Community
- What: Plenary sessions / discussions
- Contributions: 1-page abstracts
- More info: <http://homepages.vub.ac.be/~mschouke/benchmark2016.html>

# Benchmark on nonlinear system identification

25/04/2016 – 27/04/2016

**You are all invited to participate**

<http://homepages.vub.ac.be/~mschouke/benchmark2016.html>